# Mountaineering Strategy to Excited States: Highly Accurate Energies and Benchmarks for Exotic Molecules and Radicals

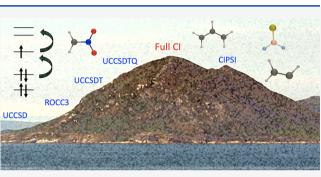
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**Abstract**: Aming at completing the sets of FCI-quality transition energies that we recently developed (*J. Chem. Theory Comput.* **2018**, *14*, 4360–4379, *ibid.* **2019**, *15*, 1939–1956, and *ibid.* **2020**, *16*, 1711–1741), we provide, in the present contribution, ultra-accurate vertical excitation energies for a series of "exotic" closed-shell molecules containing F, Cl, P, and Si atoms and small radicals, such as CON and its variants, that were not considered to date in such investigations. This represents a total of 81 high-quality transitions obtained with a series of diffuse-containing basis sets of various sizes. For the exotic compounds, these transitions are used to perform benchmarks with a vast array of lower level models, i.e., CIS(D), EOM-MP2, (SOS/SCS)-CC2,



STEOM-CCSD, CCSDR (3), CCSDT-3, (SOS-)ADC(2), and ADC(3). Additional comparisons are made with literature data. For the open-shell compounds, we compared the performance of both the unrestricted and the restricted open-shell CCSD and CC3 formalisms.

# 1. INTRODUCTION

The increase of computational ressources coupled to the emergence of more advanced algorithms has led to a resurgence of the selected configuration interaction (SCI) approaches<sup>1-3</sup> as an effective strategy to rapidly reach the full CI (FCI) limit at a fraction of the cost of a genuine FCI calculation thanks to a sparse exploration of the FCI space.<sup>4-19</sup> This revival is especially beneficial for calculation of transition energies between electronic states,<sup>6,15-23</sup> as accurate determination of these energies remains one of the great challenges faced by theoretical chemists.

Recently, we developed two sets of theoretical best estimates (TBEs) of FCI quality for the vertical transition energies of small closed-shell compounds.<sup>20,21</sup> (See ref 24 for a recent review.) In our first work,<sup>20</sup> we reported TBEs for more than 100 electronic transitions of single-excitation character in organic compounds containing from one to three nonhydrogen atoms, namely, C, N, O, and S. These TBEs have been obtained thanks to an efficient implementation of the CIPSI (configuration interaction using a perturbative selection made iteratively) SCI algorithm,<sup>19</sup> which selects the most important determinants in the FCI space using a second-order perturbative criterion.<sup>8</sup> Their quality was further confirmed by coupled-cluster (CC) calculations performed up to high excitation degrees. It turned out that CC including contributions up to the quadruples (CCSDTQ)<sup>25</sup> yields transition energies almost systematically equal to FCI, with a mean absolue error (MAE) as small as 0.01 eV, whereas the three tested CC approaches including perturbative triples,

namely, CC3,<sup>26,27</sup> CCSDT-3,<sup>28,29</sup> and CCSDT,<sup>30</sup> are also very effective with MAEs of 0.03 eV.<sup>20</sup> This means that these four CC models are (on average) chemically accurate (error smaller than 1 kcal·mol<sup>-1</sup> or 0.043 eV) for these single-excitation transitions.

Our second set encompasses 20 transitions characterized by a large and/or dominant double-excitation nature.<sup>21</sup> These types of electronic excitations are known to be much more challenging for single-reference methods. For this set, we relied again on SCI methods to determine TBEs, and we evaluated the performance of various multireference approaches, such as the second-order complete active space perturbation theory (CASPT2),<sup>31,32</sup> and the second-order *n*-electron valence state perturbation theory (NEVPT2)<sup>33-35</sup> methods. Interestingly, for excitations with a large but not dominant double-excitation character, such as the first  ${}^{1}A_{g}$  excited state of *trans*-butadiene, it turns out that the accuracy obtained with CC3 and NEVPT2 is rather similar with MAEs of ca. 0.12 eV.<sup>21</sup> In contrast, for genuine double excitations (i.e, excitations with an insignificant contribution from the single excitations) in which one photon effectively promotes two electrons, the CC3 error becomes

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extremely large (of the order of 1 eV) and multireference approaches clearly have the edge (for example, the MAE of NEVPT2 is 0.07 eV).<sup>21</sup>

To the very best of our knowledge, these two sets taken together constitute the largest ensemble of chemically accurate vertical transition energies published to date with roughly 130 transition energies of FCI quality. Despite their decent sizes and the consideration of both valence and Rydberg excited states, these sets have obvious limitations. Let us point out four of these biases: (i) only small compounds are included; (ii) some important classes of transitions, such as charge-transfer (CT) excitations, are absent; (iii) compounds including only C, N, O, S, and H atoms have been considered; (iv) these sets include only singlet—singlet and singlet—triplet excitations in closed-shell molecules.

Very recently, we made extensive efforts in order to solve the first limitation.<sup>23</sup> However, performing SCI or high-level CC calculations rapidly becomes extremely tedious when one increases the system size as one hits the exponential wall inherently linked to these methods. At this stage, we believe that circumventing the second limitation is beyond reach as clear intramolecular CT transitions only occur in (very) large molecules for which CCSDTQ or SCI calculations remain clearly out of reach with current technologies. We note, however, that intermolecular CT energies were recently obtained at the CCSDT level by Kozma and co-workers.<sup>3</sup> Therefore, the aim of the present contribution is to get rid of the two latter biases. To this end, we consider here (i) a series of closed-shell compounds including (at least) one of the following atoms, F, Cl, Si, or P; (ii) a series of radicals characterized by open-shell electronic configurations and an unpaired electron. For the sake of simplicity, we denote the first additional set as "exotic" because it includes a series of chemical species that are rather unusual for organic chemistry, e.g, H-P=S and H<sub>2</sub>C=Si. Similar compounds were included in a benchmark set by the Ortiz group.<sup>37</sup> They were, however, using experimental data as reference, which often precludes straightforward comparisons with theoretical vertical transition energies.<sup>38,39</sup> On the other hand, the second set, simply labeled as "radical", encompasses doublet-doublet transitions in radicals. We believe that the additional FCI-quality estimates that we provide in the present study for both types of compounds nicely complete our previous works and will be valuable for the electronic structure community.

#### 2. COMPUTATIONAL METHODS

Our computational protocol closely follows that of ref 20. Consequently, we only report key elements below. We refer the reader to our previous work for further information about the methodology and the technical details.<sup>20</sup> In the following, we report several statistical indicators: the mean signed error (MSE), mean absolute error (MAE), root-mean square error (RMSE), and standard deviation of the errors (SDE).

**2.1. Geometries and Basis Sets.** For the exotic set, we use CC3/*aug*-cc-pVTZ ground-state geometries obtained without the frozen-core (FC) approximation (i.e, correlating all electrons) to be consistent with our previously published geometries.<sup>20,40-42</sup> These optimizations have been performed using DALTON 2017<sup>43</sup> and CFOUR 2.1,<sup>44</sup> applying default parameters. For the open-shell derivatives, the geometries are optimized at the UCCSD(T)/*aug*-cc-pVTZ level using the GAUSSIAN16 program<sup>45</sup> and applying the TIGHT con-

vergence threshold. The Cartesian coordinates of each compound are available in the Supporting Information (SI).

Throughout this paper, we use either the diffuse-containing Pople 6-31+G(d) basis set or the Dunning *aug*-cc-pVXZ (X = D, T, O, and 5) correlation-consistent family of atomic bases.

2.2. CC Reference Calculations. The CC calculations are performed with several codes. For closed-shell molecules, CC3<sup>26,27</sup> calculations are achieved with DALTON<sup>43</sup> and CFOUR<sup>44</sup> and CCSDT calculations are performed with CFOUR<sup>44</sup> and MRCC 2017,<sup>46,47</sup> the latter code being also used for CCSDTQ and CCSDTQP. Note that all of our excited-state CC calculations are performed within the equation-of-motion (EOM) or linear-response (LR) formalism that yield equivalent excited-state energies. The reported oscillator strengths have been computed in the LR-CC3 formalism only. For open-shell molecules, the CCSDT, CCSDTQ, and CCSDTQP calculations performed with MRCC<sup>46,47</sup> do consider an unrestricted Hartree-Fock (UHF) wave function as reference. All excited-state calculations are performed, except when explicitly mentioned, in the FC approximation using large cores for the third-row atoms. All electrons are correlated for the Be atom, for which we systematically applied the basis set as included in MRCC. (We have noted differences in the definition of the Dunning bases for this particular atom depending on the software.)

2.3. Selected Configuration Interaction. All of the SCI calculations are performed within the FC approximation using QUANTUM PACKAGE<sup>19</sup> where the CIPSI algorithm<sup>3</sup> is implemented. Details regarding this specific CIPSI implementation can be found in refs 19 and 49. We use a state-averaged formalism which means that the ground and excited states are described with the same number and same set of determinants but different CI coefficients. The SCI energy is defined as the sum of the variational energy (computed via diagonalization of the CI matrix in the reference space) and a second-order perturbative correction which estimates the contribution of the determinants not included in the CI space.<sup>8</sup> By extrapolating this second-order correction to zero, one can efficiently estimate the FCI limit for the total energies and hence compute the corresponding transition energies. We estimate the extrapolation error by the difference between the transition energies obtained with the largest SCI wave function and the FCI extrapolated value. These errors are systematically reported in the tables below. Although this cannot be viewed as a true error bar, it provides a rough idea of the quality of the FCI extrapolation and estimate.

**2.4.** Other Wave Function Calculations. Our benchmark effort consists in evaluating the accuracy of vertical transition energies obtained at lower levels of theory. These calculations are performed with a variety of codes. For the exotic set, we rely on the following: GAUSSIAN<sup>45</sup> and TURBOMOLE 7.3<sup>50</sup> for CIS(D);<sup>51,52</sup> Q-CHEM 5.2<sup>53</sup> for EOM-MP2 [CCSD(2)]<sup>54</sup> and ADC(3);<sup>55–57</sup> Q-CHEM<sup>53</sup> and TURBOMOLE<sup>50</sup> for ADC(2);<sup>57,58</sup> DALTON<sup>43</sup> and TURBO-MOLE<sup>50</sup> for CC2;<sup>59,60</sup> DALTON<sup>43</sup> and GAUSSIAN for CCSD;<sup>61</sup> DALTON<sup>43</sup> for CCSDR(3);<sup>62</sup> CFOUR<sup>44</sup> for CCSDT-3;<sup>28,29</sup> and ORCA<sup>63</sup> for similarity-transformed EOM-CCSD (STEOM-CCSD).<sup>64,65</sup> In addition, we evaluate the spin-opposite scaling (SOS) variants of ADC(2) and SOS-ADC(2), as implemented in both Q-CHEM<sup>66</sup> and TURBO-MOLE.<sup>67</sup> Note that these two codes have distinct SOS implementations, as explained in ref 66. We also test the SOS and spin-component scaled (SCS) versions of CC2, as

Table 1. Excitation Energies (in eV) of the Exotic Set Obtained   aue-cc-bVTZ CBS	ion Ener§	gies (in eV a	V) of the	Exotic S	set Obtain CBS		within the FC Approximation <sup>a</sup> 6-31+G(d)	C Appros	ximation	a	aue-	aue-cc-pVDZ			-ono	aug-cc-pVTZ	
		<i>f</i> [CC3]	%T <sub>1</sub>	TBE	TBE	CC3	Т	TQ	TQP	CC3	Ľ	TQ	FCI	CC3	Γ	TQ	FCI
carbonyl fluoride	$^{1}A_{2}$		91.1	7.31 <sup>b</sup>	7.31	7.33	7.30			7.34	7.31		$7.30 \pm 0.04$	7.31	7.28		$7.32 \pm 0.05$
	${}^{3}A_{2}$		97.8	7.06 <sup>c</sup>	7.07	7.03	7.00			7.05	7.02		$7.08 \pm 0.01$	7.03	7.00		$7.04 \pm 0.10$
$CCI_2$	${}^{1}B_{1}$	0.002	93.7	2.59 <sup>c</sup>	2.57	2.71	2.70	2.70		2.69	2.69		$2.68 \pm 0.02$	2.61	2.60		
	$^{1}A_{2}$		88.3	4.40 <sup>c</sup>	4.41	4.46	4.44	4.47		4.40	4.39		$4.46 \pm 0.01$	4.35	4.33		
	${}^{3}B_{1}$		98.6	1.22 <sup>c</sup>	1.23	1.10	1.09	1.11		1.20	1.19		$1.22 \pm 0.03$	1.20	1.19		$1.22 \pm 0.05$
	${}^{3}A_{2}$		96.1	4.31 <sup>c</sup>	4.32	4.41	4.38	4.42		4.34	4.31		$4.36 \pm 0.01$	4.28	4.26		
CCIF	$^{1}A''$	0.007	93.9	3.55 <sup>c</sup>	3.54	3.66	3.66	3.66		3.63	3.62		$3.62 \pm 0.01$	3.56	3.55		$3.63 \pm 0.06$
$\mathrm{CF}_2$	$^{1}B_{1}$	0.034	94.7	5.09	5.07	5.18	5.18	5.18		5.12	5.11	5.11	$5.12 \pm 0.00$	5.07	5.06		$5.09 \pm 0.01$
	${}^{3}B_{1}$		99.1	2.77	2.78	2.71	2.70	2.71		2.71	2.70	2.71	$2.71 \pm 0.01$	2.76	2.75		$2.77 \pm 0.01$
difluorodiazirine	$^1B_1$	0.002	93.1	3.74 <sup>d</sup>	3.73 <sup>e</sup>	3.83	3.83			3.80	3.80			3.74	3.74		
	$^{1}A_{2}$		91.4	7.00 <sup>d</sup>	6.98°	7.13	7.11			7.11	7.08			7.02	7.00		
	$^1B_2$	0.026	93.3	8.52 <sup>d</sup>	8.54 <sup>e</sup>	8.51	8.52			8.45	8.46			8.50	8.52		
	${}^{3}B_{1}$		98.2	3.03	3.03 <sup>e</sup>	3.09	3.09			3.06	3.06			3.03			
	${}^{3}B_{2}$		98.9	5.44	5.46°	5.48	5.48			5.47	5.46			5.45			
	${}^{3}B_{1}$		98.4	5.80	5.81 <sup>e</sup>	5.86	5.85			5.83	5.82			5.81			
formyl fluoride	$^{1}A''$	0.001	91.2	5.96°	5.97	60.9	6.06	6.07		6.03	6.00		$6.00 \pm 0.03$	5.99	5.96		
	${}^{3}A''$		97.9	5.73 <sup>c</sup>	5.75	5.72	5.70	5.71		5.65	5.62		$5.65 \pm 0.01$	5.62	5.60		
HCCI	$^{1}A''$	0.003	94.5	1.98	1.97	2.05	2.04	2.05	2.05	2.02	2.02	2.02	$2.04 \pm 0.01$	1.97	1.97		$1.98 \pm 0.00$
HCF	$^{1}A''$	0.006	95.4	2.49	2.49	2.58	2.57	2.58	2.58	2.53	2.53	2.53	$2.54 \pm 0.00$	2.49	2.49		$2.49 \pm 0.02$
HCP	$^{1}\Sigma^{-}$		94.9	4.84	4.81	5.19	5.19	5.18	5.18	5.06	5.05	5.04	$5.04 \pm 0.00$	4.85	4.85	4.84	$4.84 \pm 0.00$
	$\nabla^1$		94.0	5.15	5.10	5.48	5.48	5.48	5.48	5.33	5.33	5.32	$5.32 \pm 0.00$	5.15	5.15		$5.15 \pm 0.00$
	$^{3}\Sigma^{+}$		98.9	3.47	3.49	3.44	3.45	3.46	3.46	3.47	3.47	3.49	$3.49 \pm 0.00$	3.45	3.45	3.46	$3.47 \pm 0.00$
	$\nabla^{3}$		98.8	4.22	4.20	4.40	4.39	4.39	4.39	4.35	4.34	4.34	$4.34 \pm 0.00$	4.22	4.21	4.21	$4.22 \pm 0.00$
OdH	$^{1}A''$	0.003	90.9	2.47	2.49	2.49	2.47	2.48	2.48	2.47	2.45	2.46	$2.46 \pm 0.00$	2.46	2.46		$2.47 \pm 0.00$
HPS	$^{1}A''$	0.001	90.3	1.59	1.61	1.57	1.55	1.56	1.56	1.60	1.59	1.59	$1.60 \pm 0.00$	1.59	1.58		$1.59 \pm 0.00$
HSiF	$^{1}A''$	0.024	93.1	3.05	3.05	3.09	3.08	3.08	3.08	3.08	3.07	3.07	$3.06 \pm 0.00$	3.07	3.06		$3.05 \pm 0.00$
SiCl <sub>2</sub>	$^{1}B_{1}$	0.031	92.1	3.91 <sup>c</sup>	3.93	3.94	3.94	3.94		3.93	3.92		$3.95 \pm 0.02$	3.90	3.88		$3.88 \pm 0.03$
	${}^{3}B_{1}$		98.7	2.48 <sup>g</sup>	2.50	2.39	2.39	2.40		2.45	2.44		$2.47 \pm 0.05$	2.48	2.47		$2.49 \pm 0.04$
silylidene	$^{1}A_{2}$		92.3	2.11	2.12	2.14	2.11	2.10	2.10	2.18	2.15	2.14	$2.14 \pm 0.00$	2.15	2.13	2.12	$2.11 \pm 0.01$
	$^1B_2$	0.033	88.0	3.78	3.80	3.88	3.87	3.88	3.88	3.81	3.80	3.80	$3.79 \pm 0.01$	3.78	3.78	3.78	$3.78 \pm 0.01$
<sup><i>a</i></sup> For each transition, we also report, on the left-hand side, the LR-CC3/ <i>aug</i> -cc-pVTZ level. We also provide the TBE/CBS estimate obtained by correcting the TBE/ <i>aug</i> -cc-pVTZ value by the difference otherwise stated, the latter has been obtained directly at the FCI/ <i>aug</i> -cc-pVTZ level. We also provide the TBE/CBS estimate obtained by correcting the TBE/ <i>aug</i> -cc-pVTZ value by the difference between CC3/ <i>aug</i> -cc-pVTZ. On the right-hand side, one finds the transition energies computed at various levels of theory. T, TQ, and TQP stand for CCSDTQ, and CCSDTQP, respectively. <sup><i>b</i></sup> FCI/ <i>6</i> -31+G(d) value of 7.33 ± 0.02 eV corrected by the difference between CCSDT/ <i>aug</i> -cc-pVTZ and CCSDT/ <i>aug</i> -cc-pVDZ value corrected by the difference between CCSDT/ <i>aug</i> -cc-pVTZ and CCSDT/ <i>aug</i> -cc-pVDZ. <sup><i>d</i></sup> CCSDT/ <i>aug</i> -cc-pVTZ value. <sup><i>c</i></sup> Corrected with the quadruple- $\xi$ basis rather than the quintuple- $\xi$ basis. <sup><i>f</i></sup> CCSDT/ <i>aug</i> -cc-pVDZ value corrected by the difference between CCSJ/ <i>aug</i> -cc-pVTZ and CCSDT/ <i>aug</i> -cc-pVTZ and CCSDT/ <i>aug</i> -cc-pVDZ. <sup><i>d</i></sup> CCSDT/ <i>aug</i> -cc-pVTZ value. <sup><i>f</i></sup> Corrected with the quadruple- $\xi$ basis rather than the quintuple- $\xi$ basis. <sup><i>f</i></sup> CCSDT/ <i>aug</i> -cc-pVDZ value corrected by the difference between CCSJ/ <i>aug</i> -cc-pVTZ and CC3/ <i>aug</i> -cc-pVDZ. <sup><i>d</i></sup> CCSDT/ <i>aug</i> -cc-pVDZ. <sup><i>d</i></sup> CCSDT/ <i>aug</i> -cc-pVDZ value. <sup><i>c</i></sup> Corrected with the quadruple- $\xi$ basis rather than the quintuple- $\xi$ basis. <sup><i>f</i></sup> CCSDT/ <i>aug</i> -cc-pVDZ value. <sup><i>f</i></sup> COSDT/ <i>aug</i> -cc-pVDZ. <sup><i>d</i></sup> CCSDT/ <i>au</i>	n, we also not a latter humon the latter humon cc-pVSZ a cc-pVSZ a latter. FfC CCSDT/4	teport, on th as been obt nd CC3/au J1/6-31+G( <i>uug</i> -cc-pVT7 ence betwe	ne left-har ained dire g-cc-pVT' d) value Z and CC en CC3/	id side, the ectly at the Z. On the $Z$ of 7.33 $\pm$ SDT/aug- aug-cc- $PV$	e FCI/aug- e FCI/aug- night-hand 0.02 eV co cc-pVDZ. ' TZ and CG	aug-cc-pV. cc-pVTZ 1 side, one f rrected by <sup>d</sup> CCSDT/ C3/aug-cc-	rZ oscillat evel. We <i>a</i> inds the tr the differ <i>aug</i> -cc-pV pVDZ. <sup>g</sup> (	or strengt ilso provi ansition e ence betv TZ value. CCSDTQ	h, the CC de the TI mergies c veen CCS - "Correct /6-31+G(	3 single-er SE/CBS er omputed a iDT/aug-c ed with th ed with th	stimate ol stimate ol tr various c-pVTZ a te quadru corrected	haracter ( ptained by levels of t und CCSI ple- $\zeta$ basis by the d	cc-pVTZ oscillator strength, the CC3 single-excitation character (%T <sub>1</sub> ), and the TBE/ <i>aug</i> -cc-pVTZ excitation energy. Exception evel. We also provide the TBE/CBS estimate obtained by correcting the TBE/ <i>aug</i> -cc-pVTZ value by the difference, one finds the transition energies computed at various levels of theory. T, TQ, and TQP stand for CCSDT, CCSDTQ, and the transition energies computed at various levels of theory. T, TQ, and TQP stand for CCSDT, CCSDTQ, and the difference between CCSDT/ <i>aug</i> -cc-pVTZ and CCSDT/ <i>aug</i> -cc-pVDZ value corrected by the difference between CCSDT/ <i>aug</i> -cc-pVDZ value. <sup>e</sup> COrrected with the quadruple-¢ basis rather than the quintuple-¢ basis. <sup>f</sup> CCSDT/ <i>aug</i> -cc-pVDZ. <i>aug</i> -cc-pVDZ. <sup>g</sup> CCSDTQ(6-31+G(d)) value corrected by the difference between CCSDT/ <i>aug</i> -cc-pVDZ.	TBE/ <i>aug</i> - TBE/ <i>aug</i> and TQP <sup>e</sup> FCI/ <i>au</i> e quintup en CCSI	cc-pVTZ e r-cc-pVTZ stand for C g-cc-pVDZ le-ζ basis. )T/aug-cc-	rxcitation e value by DCSDT, C value coi fCCSDT, PVTZ an	mergy. Except the difference CCSDTQ, and rrected by the <i>aug</i> -cc-pVDZ d CCSDT/6-
31+G(d).																	

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implemented in TURBOMOLE.<sup>50,67</sup> Discussion of various spin-scaling schemes can be found elsewhere.<sup>68</sup> When available, we take advantage of the resolution-of-the-identity (RI) approximation in TURBOMOLE and Q-CHEM. For the STEOM-CCSD calculations, it was checked that the active character percentage was, at least, 98%. When comparisons between various codes/implementations were possible, we could not detect variations in the transition energies larger than 0.01 eV. For the radical set, we applied both the U (unrestricted) and the RO (restricted open-shell) versions of CCSD and CC3 as implemented in the PSI4 code<sup>69</sup> to perform our benchmarks.

# 3. RESULTS AND DISCUSSION

3.1. Exotic Set. 3.1.1. Reference Values and Comparison to Literature. Our main results are listed in Table 1 for the exotic set that encompasses 30 electronic transitions (19 singlets and 11 triplets) in 14 molecules containing between 2 and 5 non-hydrogen atoms. Before briefly discussing the compounds individually, let us review some general trends. First, as one could expect for rather low-lying excitations, the aug-cc-pVTZ basis set is sufficiently large to provide excitation energies close to the complete basis set (CBS) limit<sup>22</sup> and the FC approximation is rather unimportant. Indeed, CC3 calculations performed with quadruple- and quintuple- $\zeta$  basis sets, with and without correlating the core electrons for the former basis, yield negligible changes as compared to the augcc-pVTZ results. As more quantitatively illustrated by the results gathered in Table S1 and Figure S1 in the SI, the maximal variation between CC3/aug-cc-pVTZ and CC3/augcc-pVQZ excitation energies is 0.03 eV ( $^{1}\Delta$  transition of HCP), and the MAE between the two basis sets is as small as 0.01 eV. The same observation applies to the FC approximation with a mean absolute variation of 0.02 eV between the CC3(full)/aug-cc-pCVQZ and CC3(FC)/aug-ccpVQZ excitation energies. Of course, using a smaller basis set than aug-cc-pVTZ, e.g., Pople's 6-31+G(d) or Dunning's augcc-pVDZ, would induce larger errors with an overestimation trend (see Figure S1). As aug-cc-pVTZ is sufficient, we do not discuss further the quadruple- and quintuple- $\zeta$  results in the following, although basis set-corrected TBEs can be found in Table 1. Second, it can be seen, from the CC3  $\%T_1$  values (which provides a measure of the amount single excitation character of the considered transition) listed in Table 1 that all of the transitions considered here are largely dominated by single excitations, the smallest  $%T_1$  being 88% (the second transition of silvlidene). Such character is favorable to ensure a rapid convergence of the CC series. This is clearly exemplified by the convergence behavior of the 6-31+G(d) excitation energies for which the CCSDTQ and the CCSDTQP transition energies are equal for the 11 cases for which the latter level of theory was achievable. Likewise, one notices that the CCSDTQ estimate systematically falls within 0.01 eV of the FCI value that comes with a very small error bar for most transitions. It is also reassuring to see that, for a given basis set, we could not detect variations larger than 0.04 eV between CCSDTQ results and their CC3 and CCSDT counterparts, the changes being typically of ca. 0.01-0.02 eV. All of these facts indicate that one can trust the FCI estimates and hence the TBEs listed in Table 1 (for the larger difluorodiazirine molecule, see discussion below).

In the spirit of the famous Thiel paper,<sup>70</sup> let us now briefly discuss each compound and compare the results to available

data. We do not intend here to provide an exhaustive review of previous calculations, which would lead to a gigantic list of references for the triatomic systems but rather to pinpoint the "best" published excitation energies to date.

Carbonyl Fluoride. For this compound encompassing four heavy atoms, the convergence of the SCI approach is rather slow and one notices a 0.03 eV drop of the transition energies between CC3 and CCSDT. We therefore used FCI estimates determined with small bases corrected for basis set effects to generate our TBEs. For the lowest singlet, which is heavily blue shifted as compared to the parent formaldehyde, the most advanced previous theoretical studies reported vertical transition energies of 7.31 [CCSDR(3)]<sup>71</sup> and 7.31 eV [MRCI+Q].<sup>72</sup> The measured EEL value is ca. 7.3 eV,<sup>72</sup> whereas the UV spectrum shows a peak at 7.34 eV.73 All of these values are obviously compatible with the current result. Note that the interpretation of the measured 0-0 values for  $F_2C=O^{74}$  is challenging, as discussed elsewhere.<sup>38</sup> For the triplet, the previous TBE is likely a 7.07 eV MRCI+Q result,<sup>77</sup> also very close to our present value, whereas there also exists estimates of the triplet adiabatic energies.<sup>7</sup>

 $CCI_2$ , CCIF, and  $CF_2$ . Dichlorocarbene is large enough to make the convergence of the SCI calculations difficult with the triple- $\zeta$  basis, and our TBEs are based on the FCI/aug-ccpVDZ values corrected for basis set effects determined at the CC level. While both CC3 and CCSDT almost perfectly reproduce the FCI results for both the singlet and triplet  $B_1$ states, more significant differences are noted for the higher lying  $A_2$  states that seem slightly too low with CCSDT. This is also confirmed by the CCSDTQ results obtained with the Pople basis set. Previous calculations are available at CCSD<sup>76</sup> and MRCI<sup>77,78</sup> levels. The most recent MRCI+Q values, obtained with a large atomic basis set, are 2.61, 4.49, 1.25, and 4.43 eV for the  ${}^{1}B_{1}$ ,  ${}^{1}A_{2}$ ,  ${}^{3}B_{1}$ , and  ${}^{3}A_{2}$  transitions, respectively. These values are reasonably close to the present TBEs. For CClF, the most accurate literature value is probably the MRCI +Q/triple- $\zeta$  estimate of 3.59 eV,<sup>79</sup> within 0.03 eV of our current TBE. For this compound, we are also aware of three previous experimental investigations focusing on its vibronic spectra.<sup>80-82</sup> For  $CF_2$ , the SCI calculations converge rapidly even with the aug-cc-pVTZ basis and yield TBEs of 5.09 and 2.77 eV for the lowest singlet and triplet transitions. There have been countless experimental and theoretical investigations for this stable carbene, but the most accurate previous estimates of the vertical transition energies are likely the 5.12 and 2.83 eV values, obtained at the MRCI+Q/aug-cc-pVTZ level of theory.<sup>83</sup>

Difluorodiazirine. This cyclopropene analogue is the largest derivative considered herein. There is a remarkable agreement between CC3 and CCSDT values, and the  $\%T_1$  value is very large for each transition, so that we consider the CC values to obtain our TBEs. For the  ${}^{1}B_{1}$  and  ${}^{3}B_{1}$  transitions, FCI/6-31+G(d) calculations deliver respective transition energies of  $3.81 \pm 0.01$  and  $3.09 \pm 0.01$  eV, perfectly consistent with the present CC values. Our TBEs are likely the most accurate to date for vertical transitions. At the GVVPT2/cc-pVTZ level, the transition energies reported in ref 84 are 2.25  $({}^{3}B_{1})$ , 2.95  $({}^{1}B_{1})$ , 4.86  $({}^{3}B_{2})$ , 5.21  $({}^{3}A_{2})$ , 6.63  $({}^{1}A_{2})$ , and 8.23 eV  $({}^{1}B_{2})$ , which follows exactly the same state ordering as the present CCSDT values. More recently, QCISD/aug-cc-pVTZ estimates of 2.81 and 3.99 eV for the lowest triplet and singlet vertical transitions have been reported, which are, respectively, slightly smaller and larger than the present data. There are also

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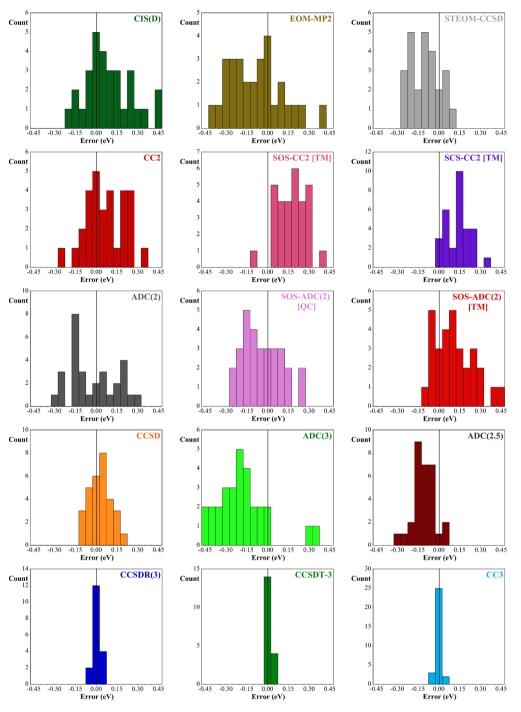


Figure 1. Histograms of the error distribution (in eV) obtained with 15 theoretical methods, choosing the TBE/*aug*-cc-pVTZ of Table 1 as references. TM and QC stand for the TURBOMOLE and Q-CHEM definitions of the scaling factors, respectively. Note the difference of scaling in the vertical axes.

quite a few studies of the 0–0 energies of various states for this derivative, both experimentally  $^{85-87}$  and theoretically.  $^{84,88,89}$ 

Formylfluoride. For this formal intermediate between carbonyl fluoride and formaldehyde, we note that the CCSDTQ/6-31+G(d) values are bracketed by their CC3 and CCSDT counterparts. The previous best estimates are likely the very recent MRCI-F12 results of Pradhan and Brown, who reported vertical transition energies of 6.03 and 5.68 eV for the  ${}^{1}A''$  and  ${}^{3}A''$  states, respectively. These energies obtained on the CCSD(T)-F12 ground-state geometries are only ca. 0.05 eV larger than the present TBEs. Most other

previous studies focused on 0–0 energies of the lowest singlet state,  ${}^{38,75,89-95}$  and it is noteworthy that CC3 reproduces the experimental 0–0 energies with high accuracy. ${}^{38,89}$  Our TBE for the singlet state (5.96 eV) is much larger than the measured 0–0 peak (4.64 eV), ${}^{93}$  which is expected for a molecule undergoing an important geometrical relaxation after excitation. ${}^{92}$ 

*HCCl, HCF, and HSiF.* For these three compounds, the SCI calculations deliver values very close to the CC estimates. For HCCl, a MRCI+Q/quintuple- $\zeta$  vertical transition energy, corrected for ground-state ZPVE effects, of 1.68 eV was

recently reported.<sup>96</sup> Given that the ZPVE energy at the MP2/ aug-cc-pVTZ level is 0.31 eV, our TBE is basically equivalent to this recent result. For HSiF, the most accurate previous estimate of the excitation energy is likely the CC3/aug-ccpVTZ 3.07 eV value,<sup>97</sup> which is extremely close to our TBE. For the records, Ehara and co-workers also investigated the 0– 0 energies and excited-state geometries of these three systems at the SAC-CI level,<sup>98</sup> and experimental 0–0 energies of 1.52 (HCCl),<sup>99</sup> 2.14 (HCF),<sup>100,101</sup> and 2.88 eV (HSiF)<sup>102</sup> have been measured.

HCP. Phosphaethyne is a linear compound for which the CC series and the SCI values do converge rapidly and give equivalent results. Consequently, one can trust the TBEs listed in Table 1. We nevertheless note that there is a significant basis set effect for the  $^{1}\Delta$  excited state that is downshifted by 0.05 eV from aug-cc-pVTZ to aug-cc-pV5Z (see Table S1 in the SI). The two most refined previous theoretical works we are aware of have been performed at the MRCI/double- $\zeta^{103}$  and CC3/ cc-pVQZ<sup>104</sup> levels of theory and, respectively, focused on reproducing the experimental vibronic couplings and understanding the HCP  $\rightarrow$  HPC isomerization process. However, somehow surprisingly, we could not find recent estimates of the vertical transition energies for phosphaethyne, the previously published data being apparently of CASSCF quality.<sup>105</sup> There are, of course, experimental characterizations of the 0-0 energies for several excited states of this compound.106

*HPO and HPS.* The lowest excited state of HPO has been studied several times in the last 20 years, <sup>89,98,107-109</sup> whereas its sulfur analogue has only been considered more recently. <sup>89,110-112</sup> In both cases, refined MRCI calculations of the vibronic spectra have been performed, <sup>98,109-112</sup> but few reported vertical transition energies. We are aware of a quite old CASPT2 estimate of 2.25 eV for HPO<sup>107</sup> and a recent MRCI vertical transition energy of 1.69 eV (obtained with a very large basis set) for HPS.<sup>112</sup>

 $SiCl_2$ . In this heavier analogue of dichlorocarbene, there are no strong methodological effect but the SCI convergence is shaky, especially for the triplet, and we used a basis setextrapolated CCSDTQ value as TBE for this state. Advanced calculations of the adiabatic energies<sup>113</sup> as well as experimental 0-0 energies<sup>114,115</sup> can be found in the literature, the latter being 3.72 and 2.35 eV for the lowest singlet and triplet states, respectively. These values are sightly larger than our vertical estimates. For the vertical singlet excitation, there is also a recent 4.06 eV CCSD//CAM-B3LYP estimate,<sup>116</sup> which slightly overshoots ours, consistent with the expected error sign of CCSD.<sup>20,70,117</sup>

*Silylidene.* One notes an excellent agreement between CCSDT, CCSDTQ, and FCI for this derivative. Our TBEs of 2.11 and 3.78 eV are again exceeding the experimental 0-0 energies of 1.88<sup>118</sup> and 3.63 eV,<sup>119</sup> as it should. The previous theoretical studies we are aware of have been performed with CISD(+Q)<sup>118,120</sup> and CC3<sup>38,89</sup> methods and mainly discussed the 0-0 energies, for which an excellent agreement with experiment was obtained by both approaches.

3.1.2. Benchmarks. Benchmarks using the TBEs obtained in the previous section can be naturally done. As we consider closed-shell compounds, there is a large number of methods that one can evaluate. Here, we have chosen 15 popular wave function methods for excited states (see Computational Details and Table S2 in the SI for the raw data). The statistical result can be found in Figure 1 and Table 2.

Table 2. Statistical Values Obtained by Comparing the Results of Various Methods to the TBE/aug-cc-pVTZ Values Listed in Table  $1^a$ 

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method	count	MSE	MAE	RMSE	SDE
CIS(D)	30	0.09	0.14	0.19	0.16
EOM-MP2	30	-0.06	0.17	0.22	0.21
STEOM-CCSD	25	-0.10	0.12	0.14	0.10
CC2	30	0.07	0.12	0.15	0.14
SOS-CC2 [TM]	30	0.17	0.18	0.20	0.10
SCS-CC2 [TM]	30	0.14	0.14	0.16	0.09
ADC(2)	30	-0.02	0.15	0.16	0.17
SOS-ADC(2) [TM]	30	0.11	0.13	0.17	0.14
SOS-ADC(2) [QC]	30	-0.04	0.12	0.14	0.14
CCSD	30	0.03	0.07	0.08	0.08
ADC(3)	30	-0.19	0.24	0.27	0.19
ADC(2.5)	30	-0.11	0.11	0.13	0.07
CCSDR(3)	19	0.01	0.02	0.02	0.02
CCSDT-3	19	0.01	0.02	0.02	0.02
CC3	30	0.00	0.01	0.02	0.02

"We report the mean signed error (MSE), mean absolute error (MAE), root-mean square error (RMSE), and standard deviation of the errors (SDE). All quantities are given in eV and have been obtained with the *aug*-cc-pVTZ basis set. TM and QC stand for the TURBOMOLE and Q-CHEM definitions of the scaling factors, respectively. ADC(2.5) is the simple average of the ADC(2) and ADC(3) transition energies, as defined in ref 121. "Count" refers to the number of transitions computed for each method.

Most of the conclusions that can be extracted from these benchmarks are consistent with recent analyses made in the field, 20,23,89,117,121-124 and we will therefore briefly comment on the most significant outcomes only. First, one notes that CC3, which is an expensive approach, is superbly accurate and consistent with a trifling MSE and a tiny SDE, whereas both CCSDT-3 and CCSDR(3), for which only singlet excited states can be evaluated with the current implementations, are also extremely satisfying with average errors well below the chemical accuracy threshold. This is unsurprisingly inline with the trends obtained for more "standard" organic compounds: CC methods including (at least partially) contributions from the triples are trustworthy for the description of single excitations.<sup>20,89,117,125–128</sup> Going down in the CC hierarchy, we find that CCSD slightly overestimates the transition energies but nevertheless provides very consistent estimates (SDE of 0.08 eV), whereas CC2 is clearly less satisfying in terms of consistency (SDE of 0.14 eV). Comparing with previous benchmarks,<sup>20,41,65,70,117,121,122,127,129,130</sup> we can foresee that the CCSD overestimation will likely grow in larger compounds, whereas the CC2 accuracy should remain less affected by the system size. The SOS and SCS variants of CC2 deliver larger MAE, with a clear overestimation (see Figure 1) but a smaller error dispersion than the standard CC2 method. The accuracy deterioration and the improved consistency of the spin-scaled CC2 versions (with respect to standard CC2) is known,<sup>68,124,131</sup> though some works reported that SOS-CC2 and SCS-CC2 can also improve the accuracy.<sup>132</sup> STEOM-CCSD delivers results of roughly CC2 quality for the present set, whereas patterns more alike those of CCSD have been previously obtained.<sup>20,23,65</sup> In the present case, both CIS(D) and EOM-MP2 [also denoted CCSD(2)], which are the two computationally lightest approaches, are also those yielding the largest dispersions alongside quite large MAEs. For EOM-MP2, similar outcomes were observed for

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VQZ	FCI			$4.13 \pm 0.01$		$2.48 \pm 0.00$	$6.46 \pm 0.00$	$1.18 \pm 0.00$	$2.90 \pm 0.00$	$3.28 \pm 0.01$	$3.96 \pm 0.01$	$5.88 \pm 0.00$	$6.96 \pm 0.00$			$1.33 \pm 0.01$	$3.21 \pm 0.00$					$3.26 \pm 0.00$	$5.80 \pm 0.00$																2.11 + 0.00
aug-cc-pVQZ	ТQ					2.48	6.46	1.18	2.90	3.29	3.97																												2.11
	Т			4.14		2.48	6.46	1.18	2.93	3.30	4.01	5.88	6.96	7.19	7.57	1.38	3.25	1.71	5.58			3.27	5.72					2.16	3.51	2.10	5.48	0.92	2.84	4.22	1.17	2.74	2.87	4.78	2.11
VTZ	FCI			$4.14 \pm 0.01$	$6.21 \pm 0.02$	$2.49 \pm 0.00$	$6.46 \pm 0.00$	$1.18 \pm 0.01$	$2.91 \pm 0.00$	$3.29 \pm 0.00$	$3.98 \pm 0.00$	$5.85 \pm 0.01$	$6.96 \pm 0.01$	$7.18 \pm 0.02$	$7.65 \pm 0.01$	$1.34 \pm 0.01$	$3.22 \pm 0.00$	$1.61 \pm 0.01$				$3.28 \pm 0.00$	$5.81 \pm 0.00$					+1	$3.49 \pm 0.01$	$2.09 \pm 0.01$	$5.42 \pm 0.07$	$0.92 \pm 0.00$	$2.80 \pm 0.02$	$4.19 \pm 0.04$	$1.16 \pm 0.01$	$2.72 \pm 0.02$	$2.83 \pm 0.05$	$4.70 \pm 0.04$	$2.12 \pm 0.00$
aug-cc-pVTZ	ТQ			4.15	6.22	2.49	6.46	1.18	2.91	3.29	3.98	5.86	6.97	7.19	7.66	1.35	3.22					3.28	5.78																2.12
	Т	3.43	4.97	4.15	6.23	2.49	6.45	1.18	2.94	3.31	4.03	5.86	6.97	7.19	7.65	1.38	3.25	1.71	5.57	3.54	4.12	3.26	5.70	0.71	2.78	0.48	2.93	2.17	3.51	2.10	5.44	0.93	2.81	4.21	1.15	2.75	2.87	4.77	2.12
	FCI	$3.44 \pm 0.04$	$4.91 \pm 0.04$	$4.20 \pm 0.09$	$6.29 \pm 0.00$	$2.52 \pm 0.00$	$6.43 \pm 0.00$	$1.21 \pm 0.00$	$2.99 \pm 0.00$	$3.32 \pm 0.00$	$4.03 \pm 0.00$	$5.79 \pm 0.00$	$7.01 \pm 0.00$	$7.18 \pm 0.00$	$7.76 \pm 0.00$	$1.38 \pm 0.00$	$3.23 \pm 0.00$	$1.58 \pm 0.00$	$5.49 \pm 0.05$	$3.54 \pm 0.01$		$3.33 \pm 0.00$	$5.90 \pm 0.00$	$0.74 \pm 0.02$	$2.88\pm0.00$	$0.53 \pm 0.00$	$3.02 \pm 0.01$	$2.23 \pm 0.00$	$3.60 \pm 0.01$	$2.13 \pm 0.01$	$5.33 \pm 0.01$	$0.96 \pm 0.00$	$2.82 \pm 0.02$	$4.28 \pm 0.02$	$1.17 \pm 0.00$	$2.80 \pm 0.00$	$2.89 \pm 0.02$	$4.76 \pm 0.01$	$2.14 \pm 0.00$
aug-cc-pVDZ	TQP			4.20	6.29	2.52	6.43	1.21	2.99	3.32	4.04	5.79	7.02	7.18	7.76	1.38	3.23					3.33	5.89																2.15
aug	ТQ			4.20	6.29	2.52	6.43	1.21	2.99	3.32	4.04	5.79	7.02	7.18	7.76	1.39	3.23	1.59	5.53			3.33	5.87					2.23	3.61	2.12	5.33	0.96	2.82	4.28	1.16	2.80	2.86	4.76	2.15
	Т	3.46	4.88	4.21	6.30	2.52	6.43	1.21	3.01	3.34	4.07	5.78	7.01	7.17	7.76	1.42	3.25	1.66	5.59	3.55	4.05	3.30	5.78	0.72	2.86	0.50	2.96	2.23	3.61	2.12	5.32	0.96	2.80	4.28	1.16	2.81	2.87	4.80	2.15
	FCI	$3.42 \pm 0.02$	+I	$4.28 \pm 0.00$	$6.32 \pm 0.00$	$2.53 \pm 0.00$	$6.42 \pm 0.00$	$1.19 \pm 0.00$	$3.05 \pm 0.00$	$3.35 \pm 0.00$	$4.09 \pm 0.00$	$6.00 \pm 0.00$	$7.28 \pm 0.00$	$7.43 \pm 0.00$		$1.40 \pm 0.00$	$3.23 \pm 0.01$	$1.57 \pm 0.00$	$5.54 \pm 0.02$	$3.53 \pm 0.00$		$3.33 \pm 0.00$	$5.82 \pm 0.00$	$0.72 \pm 0.00$	$2.87 \pm 0.00$	$0.48 \pm 0.00$		+1	+I		$5.47 \pm 0.00$	+1	$2.88\pm0.01$	$4.31 \pm 0.00$	$1.11 \pm 0.00$	$2.87 \pm 0.00$	$2.88 \pm 0.00$	$4.76 \pm 0.00$	$2.18 \pm 0.00$
6-31+G(d)	TQP			4.28	6.31	2.53	6.42	1.19	3.05	3.35	4.10	6.00	7.28	7.43	7.81	1.41	3.23					3.33	5.82					2.28	3.62	2.18	5.47	0.99	2.86	4.30	1.10	2.87			2.18
6-3	ТQ	3.44	5.14	4.28	6.31	2.53	6.42	1.19	3.05	3.35	4.10	6.00	7.28	7.43	7.81	1.41	3.23	1.59	5.56	3.50	3.79	3.33	5.79					2.28	3.62	2.17	5.47	0.99	2.86	4.30	1.10	2.87	2.87	4.76	2.18
	Т	3.46	5.16	4.29	6.32	2.53	6.42	1.19	3.07	3.36	4.12	6.00	7.28	7.43	7.81	1.44	3.24	1.66	5.62	3.54	4.04	3.30	5.69	0.73	2.85	0.49	3.07	2.27	3.62	2.18	5.45	0.99	2.85	4.30	1.10	2.88	2.87	4.80	2.19
CBS	TBE			4.13 <sup>c</sup>		2.48 <sup>c</sup>	6.46 <sup>c</sup>	$1.18^{d}$	$2.90^{d}$	3.28 <sup>d</sup>	3.96 <sup>d</sup>	5.88 <sup>d</sup>	6.96 <sup>d</sup>	7.17 <sup>e</sup>	7.48 <sup>e</sup>	1.33 <sup>c</sup>	3.21 <sup>c</sup>	1.61	5.50 <sup>g</sup>			3.26 <sup>c</sup>	5.80 <sup>c</sup>					2.14	3.49	2.09	5.49 <sup>k</sup>	0.91 <sup>f</sup>	2.83	4.22 <sup>k</sup>	$1.18^{\prime}$	$2.71^{f}$	$2.89^{k}$	$4.74^{k}$	2.11 <sup>d</sup>
AVTZ	TBE	3.39 <sup>b</sup>	4.99 <sup>b</sup>	4.14	6.21	2.49	6.46	1.18	2.91	3.29	3.98	5.85	6.96	7.18	7.65	1.34	3.22	1.61	5.49 <sup>b</sup>	$3.53^{i}$	3.86	3.28	5.81	0.73 <sup>i</sup>	$2.80^{i}$	0.51 <sup>i</sup>	2.99	2.15	3.49	2.09	5.45 <sup>i</sup>	0.92	2.80	$4.21^{i}$	1.16	2.72	2.89 <sup>i</sup>	4.73 <sup>i</sup>	2.12
		${}^{2}B_{1}$	$^{2}A_{1}$	$\Pi^2$	$^{2}\Sigma^{+}$	$\Pi^2$	$\Pi^2$	$^2B_1$	$\Delta^2$	$^{2}\Sigma^{-}$	$^{2}\Sigma^{+}$	${}^{2}A_{1}{}'$	$^{2}E'$	$^{2}E'$	${}^{2}A_{2}''$	$\Pi^2$	$^{2}\Sigma^{+}$	$^{2}\Sigma^{+}$	$\Pi^2$	$^{2}\Pi^{h}$	$^{2}\Sigma^{+h}$	$\Pi^2$	$^{2}\Sigma^{+}$	$^2B_1$	$^{2}A_{1}$	$^2B_1$	$^{2}A_{1}$	$^2B_1$	$^{2}A_{1}$	$^{2}A''$	$^{2}A'$	$^{2}A''$	$^{2}A''$	$^{2}A'$	$^{2}A''$	$^{2}A'$	$^{2}\Sigma^{+}$	$\Pi^2$	$^{2}A_{1}$
		allyl		BeF		BeH		$\mathrm{BH}_2$	CH			CH <sub>3</sub>				CN		CNO		CON		CO+		$F_2BO$		$F_2BS$		$H_2BO$		HCO		НОС	$H_2PO$		$H_2PS$		NCO		NH,

continued
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Table

			CDS		Ó	٥-31+9(٩)			ถึงห	aug-u-pv d			nug-u-pv 1 2	V12		aug-cc-pVUL	777
		TBE	TBE	Т	ТQ	TQP	FCI	Т	ТQ	TQP	FCI	Т	ТQ	FCI	Т	ТQ	FCI
	${}^{2}A_{2}$	2.38 <sup>1</sup>		2.40			$2.39 \pm 0.01$	2.39				2.38					
	$^{2}A_{1}$	2.56 <sup>1</sup>		2.64				2.58				2.56					
	${}^2B_1$	5.35 <sup>1</sup>		5.48				5.39				5.35					
NO	$^{2}\Sigma^{+}$	6.13	6.12	6.12	6.11	6.11	$6.11 \pm 0.00$	6.03	6.02	6.02	$6.03 \pm 0.01$	6.13	6.12	$6.13 \pm 0.02$	6.12		
	$^{2}\Sigma^{+}$	7.29 <sup>m</sup>	7.21 <sup>n</sup>	7.59	7.59	7.59		7.34	7.34	7.34		7.29	7.29		7.21		
НО	$^{2}\Sigma^{+}$	4.10	4.09 <sup>d</sup>	4.28	4.28	4.28	$4.28 \pm 0.00$	4.16	4.16	4.16	$4.16 \pm 0.00$	4.12	4.12	$4.10 \pm 0.01$	4.11	4.10	$4.10 \pm 0.00$
	$^{2}\Sigma^{-}$	8.02	8.11 <sup>d</sup>	8.83	8.83	8.83	$8.83 \pm 0.00$	7.88	7.88	7.88	$7.88 \pm 0.00$	8.04	8.02	$8.02 \pm 0.00$	8.10	8.09	$8.09 \pm 0.00$
$PH_2$	$^{2}A_{1}$	2.77	2.76 <sup>d</sup>	2.90	2.90	2.90	$2.90 \pm 0.00$	2.79	2.79	2.79	$2.79 \pm 0.00$	2.77	2.77	$2.77 \pm 0.00$	2.76	2.76	$2.76 \pm 0.00$
vinyl	$^{2}A''$	3.26		3.45	3.43	3.43	$3.43 \pm 0.00$	3.36	3.34		$3.35 \pm 0.00$	3.31		$3.26 \pm 0.02$			
	$^{2}A''$	4.69		4.98	4.96	4.96	$4.96 \pm 0.00$	4.80			$4.78 \pm 0.01$	4.73		$4.69 \pm 0.02$			
	$^{2}A'h$	5.60		5.83	5.75	5.75	$5.74 \pm 0.01$	5.75	5.67		$5.68 \pm 0.00$	5.74		$5.60 \pm 0.01$			
	$^{2}A'$	6.20 <sup>b</sup>		6.50	6.48	6.48	$6.49 \pm 0.01$	6.15	6.14			6.21					

respectively. <sup>b</sup>FCI/6-31+G(d) value corrected by the difference between CCSDT/aug-cc-pVTZ and CCSDT/6-31+G(d). <sup>c</sup>FCI/aug-cc-pVQZ value. <sup>d</sup>FCI/aug-cc-pVQZ value corrected by the 31+G(d); <sup>th</sup>For these challenging states, ROCC rather than UCC is used. <sup>t</sup>FCI/*aug*-cc-pVDZ value corrected by the difference between CCSDT/*aug*-cc-pVDZ. <sup>J</sup>CCSDTQ/6-31+G(d) value corrected by the difference between CCSDT/*aug*-cc-pVTZ and CCSDT/6-31+G(d). <sup>k</sup>FCI/*aug*-cc-pVDZ value corrected by the difference between CCSDT/*aug*-cc-pVQZ and CCSDT/ *aug*-cc-pVDZ. <sup>I</sup>CCSDT/*aug*-cc-pVTZ value. <sup>m</sup>CCSDTQ/*aug*-cc-pVTZ value corrected by the difference between CCSDT/*aug*-cc-pVQZ and CCSDT/ *aug*-cc-pVDZ. <sup>I</sup>CCSDT/*aug*-cc-pVTZ value. <sup>m</sup>CCSDTQ/*aug*-cc-pVTZ value corrected by the difference between CCSDT/*aug*-cc-pVQZ and CCSDT/*aug*-cc-pVTZ. the largest affordable basis set On the right-hand side, one finds the transition energies computed at various levels of theory. T, TQ, and TQP stand for JUCCSDT, UCCSDTQ, and UCCSDTQP, CCSDT/aug-cc-pVTZ. <sup>f</sup>FCI/aug-ccpVTZ value corrected by the difference between CCSDT/aug-cc-pVQZ and CCSDT/aug-cc-pVTZ. 8FCI/6-31+G(d) value corrected by the difference between CCSDT/aug-cc-pVQZ and CCSDT/6-FCI/aug-cc-pVTZ value corrected by the difference between CCSDT/aug-cc-pVSZ and difference between CCSDT/aug-cc-pV5Z and CCSDT/aug-cc-pVQZ. Å

valence excited states by Tajti and Szalay,<sup>123</sup> whereas the relatively poor performance of CIS(D) is well documented.<sup>20,23,68,131</sup> In the ADC series, we note that ADC(2) yields results only slightly less accurate than CC2 for a smaller computational cost, which is consistent with the conclusions of Dreuw's group,<sup>56</sup> whereas the SOS variant developed by the same group<sup>66</sup> has a slight edge over its TURBOMOLE variant. ADC(3) provides rather poor excitation energies, a trend we recently evidenced in other molecular sets.<sup>20,121,128</sup> Finally, the very recently introduced ADC(2.5) scheme, which corresponds to the simple average of the ADC(2) and ADC(3) excitation energies,<sup>121</sup> provides significantly more consistent estimates than both ADC(2) or ADC(3) with a SDE of 0.07 eV only compared to ca. 0.18 eV for the "parent" methods. ADC(2.5) can then be seen as a cost-effective approach to improve upon ADC(3), at least for small compounds.

3.2. Radical Set. 3.2.1. Reference Values and Comparison to the Literature. Let us now turn to radicals. As nicely summarized by Crawford 15 years ago,<sup>133</sup> electronic transitions in open-shell systems are more challenging, not only due to the more limited number of methods and codes available for treating them (as compared to closed-shell molecules) but also because (i) strong spin contamination can take place with "low"-level methods, (ii) large contributions from doubly excited configurations are quite common, and (iii) basis set effects can be very large, meaning that reaching the CBS limit can be laborious. At the CCSD level, for instance, significant differences between U and RO transition energies can sometimes be observed.<sup>133</sup> This is why our results, listed in Table 3, use as computationally lightest approach the (U)CCSDT method, so that the wave function is robust enough in order to mitigate the two former issues for most of the considered transitions. As can be seen in the 6-31+G(d)and aug-cc-pVDZ columns of Table 3, one generally finds an excellent agreement between the various CC estimates and their FCI counterparts, UCCSDT being already extremely accurate except in specific cases (such as the  ${}^{2}\Sigma^{+}$  excited state of CO+). This overall consistency indicates yet again that one can trust the present TBEs. Figure S2 in the SI provides histograms of the errors obtained when comparing CCSDT results obtained with 6-31+G(d), aug-cc-pVDZ, and aug-ccpVTZ to their aug-cc-pVQZ counterparts. While some large errors can be noticed with the Pople basis set, one notes a relatively satisfying behavior of aug-cc-pVDZ. More importantly, the accuracy of aug-cc-pVTZ is clearly confirmed. We also underline that except for diatomics, UCCSDT calculations performed with diffuse basis sets on open-shell molecules are quite rare in the literature (see below), and the same obviously holds for higher order CC. As for the exotic set, we do not intend here to provide an exhaustive list of previous works but rather to pinpoint a few interesting comparisons with earlier accurate estimates.

*Allyl.* For the lowest valence  $(B_1)$  and Rydberg  $(A_1)$  transitions of the allyl radical, the previous TBEs are likely the ROCC3 3.44 and 4.94 eV vertical transition energies obtained by the Crawford group with the *aug*-cc-pVTZ basis further augmented with molecule-centered functions (mcf).<sup>134</sup> For the lowest state, a very similar value of 3.43 eV was obtained at the ROCC3 level without mcf.<sup>89</sup> The present work is the first to report CCSDT and CCSDTQ results. They clearly show that these previous ROCC3 estimates are very accurate. In addition, our TBEs of 3.39 and 4.99 eV are reasonably consistent with earlier CASPT2 (3.32 and 5.11 eV)<sup>135</sup> and

MRCI (3.32 and 4.68 eV)<sup>136</sup> data. The experimental 0–0 energies have been reported to be  $3.07^{137}$  and  $4.97 \text{ eV}^{136,138}$  for the  ${}^{2}B_{1}$  and  ${}^{2}A_{1}$  states, respectively. The fact that the experimental  $T_{0}$  value is very close to the computed vertical transition energy of the second state is rather surprising but remains unchanged with the present estimates.

*BeF.* In this compound, CCSDT delivers transition energies in very good agreement with FCI (and higher CC levels), but one notices a non-negligible basis set effect for the second transition of Rydberg character. This transition becomes significantly mixed in very large basis sets, making a clear attribution difficult. For this derivative (and other diatomics), experimental vertical transition energies can be calculated by analyzing the experimental spectroscopic constants.<sup>139</sup> Our TBE/*aug*-cc-pVTZ values of 4.14 and 6.21 eV are obviously close to the measured values of 4.14 and 6.16 eV.<sup>139</sup> For the lowest state, a previous MRCI value of 4.23 eV can be found in the literature.<sup>140</sup> There is also a recent evaluation of the adiabatic energies for numerous excited states at the MRCI+Q level.<sup>141</sup>

*BeH.* The convergences with respect to both the CC excitation order and the basis set size are extremely fast for this five-electron system. A previous study reports FCI values for many excited states<sup>142</sup> and, in particular, excitation energies of 2.53 and 6.30 eV for the two <sup>2</sup>II states considered herein. The experimental vertical transition energies are 2.48 and 6.32 eV.<sup>139</sup> Our larger value associated with the second transition is likely a consequence of the UCCSD(T) geometry, which delivers a slightly too short bond length (1.321 vs 1.327 Å experimentally).

 $BH_2$ ,  $NH_2$ , and  $PH_2$ . In these three related compounds, convergence with respect to the CC excitation order and basis set size is also very fast, so that accurate estimates can be easily produced for the lowest lying transition: With the aug-ccpVTZ basis set, near-CBS excitation energies of 1.18, 2.12, and 2.77 eV for the boron, nitrogen, and phosphorus derivatives are, respectively, obtained. For  $BH_2$ , a previous MRCI estimate of 1.10 eV is available in the literature.<sup>143</sup> We note that for  $BH_2$ the geometry relaxation of the bent ground-state structure would lead to a linear geometry in its lowest excited state,<sup>144</sup> a phenomenon that was extensively studied both experimentally and theoretically (see ref 144 and references therein). For NH<sub>2</sub>, a vertical estimate of 2.18 eV was reported by Szalay and Gauss using a CCSD approach including "pseudo"-triple <sup>45</sup> and high-order CC calculations were later excitations,<sup>12</sup> performed by Kallay and Gauss to investigate the structures and energetics of the ground and excited states.<sup>146,147</sup> For PH<sub>2</sub>, the most detailed ab initio studies that are available in the literature focus on the 0-0 energies and rovibronic spectra,<sup>148-150</sup> except for a recent report listing a ROCC3 vertical transition energy of 2.75 eV,<sup>89</sup> obviously close to the present TBE.

*CH.* For the three considered transitions, the CCSDT values are slightly too large, whereas the basis set effects are rather usual with nearly converged results for the *aug*-cc-pVTZ basis set. Although we consider a theoretical geometry, our basis set-corrected TBEs of 2.90, 3.28, and 3.96 eV for the  ${}^{2}\Delta$ ,  ${}^{2}\Sigma^{-}$ , and  ${}^{2}\Sigma^{+}$  states are all extremely close to the vertical experimental values of 2.88, 3.26, and 3.94 eV. ${}^{139,151}$  There are many previous works on the CH radical, and it is interesting to mention that the ROCCSD values are 3.21, 4.25, and 5.22 eV for the same three states,  ${}^{145}$  whereas the corresponding ROCC3 results are 3.16, 3.58, and 4.47 eV; ${}^{133}$  and the

*CH*<sub>3</sub>. For the methyl radical, the convergence of the CC excitation energies and the near-perfect agreement between CC and FCI is worth noting. Nonetheless, large basis set effects are present for the transition energies, especially for the high-lying  ${}^{2}A_{2}''$  state for which the *aug*-cc-pVTZ excitation energy is still far from being converged basis set wise. Our TBEs, including corrections up to quintuple- $\zeta$ , are 5.88, 6.96, 7.17, and 7.48 eV for the four lowest transitions. These values can be compared to the previous MRCI estimates<sup>154,155</sup> of 5.86 (5.91), 6.95 (7.03), 7.13 (-), and 7.37 (7.66) eV reported in refs 154 (155). The experimental  $T_{0}$  value is 5.73 eV for the  ${}^{2}A_{1}''$  state,<sup>157,158</sup> both slightly below our FCI vertical estimates.

*CN*. Both methodological and basis set effects are firmly under control for the cyano radical, so that our FCI/*aug*-ccpVTZ results of 1.34 and 3.22 eV for the lowest excited states are likely very accurate for the considered geometry. These values are indeed close to the experimental energies of 1.32 and 3.22 eV.<sup>139</sup> One can find careful MRCI studies<sup>159,160</sup> as well as an extensive benchmark<sup>161</sup> for the adiabatic energies of this radical.

CNO, CON, and NCO. Inspired by a previous investigation,<sup>159</sup> we evaluated the two lowest doublet transitions in these three linear isomers. For CNO-the second most stable isomer-one notes non-negligible drops of the transition energies going from CCSDT to CCSDTQ, the latter theory providing data in perfect match with the FCI results. Our TBEs of 1.61 ( $^{2}\Sigma^{+}$ ) and 5.50 eV ( $^{2}\Pi$ ) do compare very favorably with the corresponding MRCI+Q results of 1.66 and 5.50 eV, respectively.<sup>159</sup> For the former transition, there is also a ROCC3 vertical transition energy of 1.71 eV<sup>89</sup> and a detailed rovibronic investigation<sup>162</sup> available in the literature. The data are much scarcer for CON, and the only previous work we are aware of reports potential energy surfaces without listing explicitly the transition energies.<sup>159</sup> For CON, we performed multireference calculations to identify the lowest states (see Table S4 in the SI). The NEVPT2 calculations locate the  ${}^{2}\Pi$ and  $^{2}\Sigma^{+}$  transitions at 3.52 and 3.81 eV, respectively, similar values being obtained with both CASPT2 and MRCI. As can be seen in Table 3 the FCI-based estimate of 3.53 eV for the former transition is extremely consistent. For the latter transition, the difference between CCSDT and CCSDTQ energies is as large as -0.25 eV, suggesting that further corrections would be required. Nevertheless, our CC-derived TBE of 3.86 eV is rather consistent with the NEVPT2 and MRCI values. For NCO, the most stable of the three isomers, the basis set effects are trifling, but CCSDTQ is again mandatory in order to obtain a very accurate transition energy for the  ${}^{2}\Pi$  state. This compound was studied previously at the MRCI+Q level, a method which delivers respective vertical transition energies of 2.89 and 4.68 eV for the  ${}^{2}\Sigma^{+}$  and  ${}^{2}\Pi$ states,<sup>159</sup> whereas the ROCC3/*aug*-cc-pVTZ transition energy of the lowest excited state is 2.83 eV.<sup>89</sup> The measured experimental 0–0 energies are  $2.82^{163}$  and 3.94 eV.<sup>164</sup> All of these data are quite consistent with our new values of 2.89 and 4.74 eV.

CO<sup>+</sup>. Our FCI/*aug*-cc-pVQZ values for the  ${}^{2}\Pi$  and  ${}^{2}\Sigma^{+}$  transitions, 3.26 and 5.80 eV, are clearly matching the experimental values of 3.26 and 5.81 eV.<sup>139</sup> While basis set effects are rather standard for this radical cation, it is noteworthy that the CC expansion converges slowly for the Rydberg  ${}^{2}\Sigma^{+}$  transition: one needs CCSDTQP to be within 0.01 eV of the FCI result! Nonetheless, previous ROCC3 (3.29 and 5.73 eV)<sup>133</sup> and ROCC(2,3) data (3.35 and 5.81 eV)<sup>151</sup> also fall within ±0.10 eV of the present TBEs.

*F*<sub>2</sub>*BO* and *F*<sub>2</sub>*BS*. These two radicals present a very low-lying  $\pi$ -*n* transition, which is described very similarly by all basis sets used in Table 3. For these transitions our TBEs are 0.73 (F<sub>2</sub>BO) and 0.51 (F<sub>2</sub>BS) eV, whereas for the second transition of  $\sigma$ -*n* nature, our TBEs are 2.80 (F<sub>2</sub>BO) and 2.99 (F<sub>2</sub>BS) eV. For these two compounds, the most advanced previous results are likely the ROCC3/*aug*-cc-pVTZ values of 0.71 and 2.78 eV (F<sub>2</sub>BO) and 0.47 and 2.93 eV (F<sub>2</sub>BS) obtained by some of us in a recent study.<sup>89</sup> For the former radical, these values are also very close to earlier CASPT2 (0.70 and 2.93 eV)<sup>165</sup> and SAC-CI (0.73 and 2.89 eV)<sup>166</sup> estimates. The  $T_0$  energies of these two states were both measured recently as well: 0.65 and 2.78 eV for the oxygen derivative<sup>167</sup> and 0.44 and 2.87 eV for the sulfur radical.<sup>168</sup> These two works and an earlier study by the same group<sup>169</sup> also provide advanced theoretical studies of both the 0–0 transitions and the vibronic couplings.

*H*<sub>2</sub>*BO*. This lighter analogue of F<sub>2</sub>BO remains to be detected experimentally, but its excited states have been studied twice with ab initio theoretical methods, <sup>166,169</sup> the most recent SAC–CI estimates for the lowest lying transitions being 2.08 and 3.49 eV.<sup>166</sup> These SAC–CI excitation energies are within 0.10 eV of our FCI-based TBEs.

HCO and HOC (formyl and isoformyl). For the formyl radical, our TBEs are 2.09 and 5.49 eV. Kus and Bartlett reported CCSDT/6-311++G(d,p) transition energies of 2.17 and 5.29 eV (likely the best vertical estimates available previously),  $^{170}$  obviously close to ours for the former valence transition. We are also aware of earlier CASPT2 estimates of 2.07 and 5.45 eV for these two states,<sup>171</sup> which happen to be within  $\pm 0.04$  eV of our TBEs. There are detailed studies of the potential energy surfaces for the ground and lowest excited states of HCO.<sup>172</sup> For isoformyl, the convergence with respect to the basis set is fast and the lowest excited state is well converged with our FCI approach. Hence, we propose a safe TBE of 0.91 eV for the lowest vertical excitation. Most previous studies did not, once more, discuss vertical transition energies. However, we are aware of a recent 0.87 eV CC estimate for the adiabatic energy obtained with a large basis set.<sup>17</sup>

 $H_2PO$  and  $H_2PS$ . These two radical homologues of formaldehyde are puckered in their ground state, and CCSDT is already giving very accurate estimates. Indeed, the CCSDT values are consistent with their FCI counterparts, and one likely needs a triple- $\zeta$  basis set to be close to convergence. The only previous experimental and theoretical studies we are aware of for these two compounds are rather recent.<sup>89,174,175</sup> They reported (i) CCSD/*aug*-cc-pVTZ adiabatic energies of 1.42 and 3.32 eV for H<sub>2</sub>PO<sup>174</sup> and 0.57 and 2.58 eV for its sulfur counterpart<sup>175</sup> and (ii) ROCC3 vertical transitions to the lowest <sup>2</sup>A' states of 4.35 eV (H<sub>2</sub>PO) and 2.78 eV (H<sub>2</sub>PS).<sup>89</sup> The latter are obviously compatible with the present data.

*Nitromethyl.* For this (comparatively) large derivative, even the UCCSDT/*aug*-cc-pVTZ calculations are a challenge in

terms of computational resources. The calculations converge too slowly with the number of determinants to ensure valuable FCI extrapolations, except for the second state for which the CCSDT estimate falls within the extrapolation error bar. Fortunately, for all transitions, the difference between ROCC3 and UCCSDT estimates are small, and we can propose our CCSDT values as references. These values of 2.05, 2.38, 2.56, and 5.35 eV do agree rather well with the 2005 ROCC3/ Sadlej-TZ estimates of 2.03, 2.41, 2.53, and 5.28 eV,<sup>133</sup> which remain the most advanced carried out previously to the very best of our knowledge. Retrospectively, the MRCI excitation energies of 1.25 and 1.52 eV for the two lowest states seem way too low.<sup>176</sup> The measured photoelectron spectrum of the related anion indicates the presence of the  ${}^{2}A_{2}$  transition at 1.59 eV in the radical,<sup>177</sup> whereas a rough estimate of 4.25 eV can also be deduced from experimental data for the  ${}^{2}B_{1}$ state.<sup>178</sup> We trust that the TBEs given in Table 3 are more trustworthy estimates of the vertical transition energies than these indirect experimental transition energies.

*NO*. This highly reactive radical is unsurprisingly quite difficult to capture with theoretical approaches, and our current TBEs of 6.12 and 7.21 eV for the two lowest Rydberg states are significantly above the vertical experimental energies of 5.93 and 7.03 eV.<sup>139</sup> Our geometry is associated with a NO bond distance of 1.149 Å, slightly larger than the experimental value of 1.115 Å. Moreover, basis set convergence is slow, so that a quadruple- $\zeta$  basis might still be insufficient to be close to the CBS limit for the second excited state.

*OH.* For OH, the convergence of the CC energy with respect to the excitation degree is extremely fast but the basis set effects are non-negligible. Our TBEs are 4.09 and 8.11 eV for the  ${}^{2}\Sigma^{+}$  and  ${}^{2}\Sigma^{-}$  transitions, respectively. The former value compares very nicely with the experimental one  $(4.08 \text{ eV})^{139}$  and is smaller than previous MRCI estimates of  $4.27^{179}$  and 4.22 eV.<sup>145</sup> In contrast, for the  ${}^{2}\Sigma^{-}$  transition, our estimate is higher than a previously reported value of 7.87 eV.<sup>179</sup>

Vinyl. For this final radical, we considered four states, two in each spatial symmetry. For the lowest transition of  $\pi \rightarrow n$ nature, our FCI/aug-cc-pVTZ result is  $3.26 \pm 0.02$  eV, and one can find many previous calculations yielding similar transition energies, 3.17 (MRCI),  $^{180} 3.24 \text{ (MRCI)}$ ,  $^{181} 3.31 \text{ (CCSD)}$ ,  $^{182}$ and 3.30 eV (CC3),  $^{89}$  whereas the measured 0–0 energy is 2.49 eV.<sup>183</sup> For the second transition of the same A'' symmetry and of  $n \rightarrow \pi^*$  character, the previous theoretical values we are aware of are: 4.78 (MRCI)<sup>181</sup> and 4.93 eV (CCSD).<sup>182</sup> Our TBE of 4.69 eV is lower. The lowest  ${}^{2}A'$  transition is a tricky valence excitation of  $\pi \rightarrow \pi^*$  character with a significant multiexcitation character, and we decided to use ROCC for this specific case. It is clear from Table 3 that one needs to go as high as CCSDTQ to be close to FCI. Our TBE of 5.60 eV can be compared to previous estimates of 5.58 (MRCI)<sup>181</sup> or 5.60 eV (spin-flip CCSD),<sup>182</sup> which clearly highlights the fantastic accuracy of the spin-flip approach for such transition. Eventually, the last transition of Rydberg character is easier to describe at the CC level, with our TBE of 6.20 eV again close to previously reported results: 6.25 (MRCI)<sup>181</sup> and 6.31 eV (CCSD).<sup>182</sup>

3.2.2. Benchmarks. As for the exotic set, we used our TBEs/aug-cc-pVTZ to perform benchmarks of "lower order" methods, and we especially compared the U and RO versions of CCSD and CC3, considering all transition energies listed in Table 3 (except three particularly challenging ones that have been omitted, see footnote h in Table 3). The raw data are

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listed in Table S3 of the SI, whereas Table 4 and Figure 2 gather the associated statistical data. As expected from previous

Table 4. Statistical Values Obtained by Comparing the Results of Various Methods to the TBE/*aug*-cc-pVTZ Reported in Table 3 (raw data in Table S3)<sup>*a*</sup>

1	method	count	MSE	MAE	RMSE	SDE
U	ICCSD	48	0.19	0.20	0.35	0.30
R	OCCSD	48	0.14	0.15	0.30	0.27
U	ICC3	48	0.03	0.06	0.11	0.11
R	OCC3	48	0.02	0.05	0.10	0.10
<sup>a</sup> See	e caption of	Table 2 fo	or more de	tails.		

RO-CCSD **U-CCSI** Coun Count -0.60 -0.45 -0.30 -0.15 0-0.60 -0.45 -0.30 -0.15 0.00 0.15 0. 0.00 0.15 Error (eV) Error (eV) U-CC3 RO-CC3 Count Count 0.00 0.15 0.30 0.45 0.60 0-0.60 -0.45 -0.30 -0.15 0.00 .30 0.45 0.60 0 60 -0 45 -0 30 -0 15 0.15 Error (eV) Error (eV)

**Figure 2.** Histograms of the error distribution (in eV) obtained with four theoretical methods choosing the TBE/*aug*-cc-pVTZ of Table 3 as reference (raw data in Table S3). For CCSD, even larger errors (out of scale) are observed.

works,<sup>89,133,182</sup> the excitation energy errors associated with these doublet-doublet transitions in open-shell molecules tend to be larger than for closed-shell systems. Indeed, we note that (i) CCSD overshoots by more than 1 eV the transition energies of the second and third excited states of CH, (ii) the MAE obtained with CC3 is 0.05 eV, five times larger than in the exotic set, and (iii) the error dispersion is obviously larger in Figure 2 than in Figure 1. This confirms that accurately describing doublet-doublet transition energies is challenging. On a more positive note, we observe that the statistical results are improved using a RO starting point instead of the usual U approximation, an effect particularly significant at the CCSD level.

## 4. CONCLUSIONS

In order to complete our three previous sets of highly accurate excitation energies,<sup>23,38,39</sup> we reported here two additional sets of TBEs for (i) 30 excited states in a series of "exotic" closed-shell compounds including (at least) F, Cl, Si, or P, and (ii) 51 doublet—doublet transitions in a series of radicals characterized by an open-shell electronic configuration. In all cases, we reported at least *aug*-cc-pVTZ estimates, the vast majority being obtained at the FCI level, and we applied increasingly accurate CC methods to ascertain these estimates. For most of these transitions, it is very likely that the present TBEs are the

most accurate vertical energies published to date (for a given geometry).

For the former exotic set, these TBEs have been used to assess the performances of 15 "lower-order" wave function approaches, including several CC and ADC variants. Consistent with our previous works, we found that CC3 is astonishingly accurate with a MAE as small as 0.01 eV and a SDE of 0.02 eV, whereas the trends for the other methods are similar to that obtained on more standard organic compounds. In contrast, for the radical set, even the refined ROCC3 method yields a MAE of 0.05 eV and a rather large SDE of 0.10 eV. Likewise, the excitation energies obtained with CCSD are much less satisfying for open-shell derivatives (MAE of 0.20 eV with UCCSD and 0.15 eV with ROCCSD) than for the closed-shell systems (MAE of 0.07 eV).

We hope that these two new sets, which provide a fair ground for the assessments of high-level excited-state models, will be additional valuable assets for the electronic structure community and will stimulate further developments in the field.

# ASSOCIATED CONTENT

#### **1** Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jctc.0c00227.

Basis set effects at the CC3 level for the exotic set; analysis of basis set effects; benchmark data; multireference values for CON; Cartesian coordinates (PDF)

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#### Notes

The authors declare no competing financial interest.

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